

AM1b, a.a. 2002-2003 - Esercizi 2

Silvia Mataloni, Giampiero Palatucci

19 marzo 2003

Calcolare i seguenti limiti di funzioni:

1. $\lim_{x \rightarrow +\infty} \frac{x^2 + 5}{2x^3 + 1}, \quad \lim_{x \rightarrow +\infty} \frac{x^2 - 1}{x^4}, \quad \lim_{x \rightarrow +\infty} \frac{x^4 - 2x}{x^3 + 2}, \quad \lim_{x \rightarrow -\infty} \frac{2x^3 + 1}{3 - x^2}, \quad \lim_{x \rightarrow +\infty} \frac{x^4 - 2x^2 + 1}{x^2 - 1}, \quad \lim_{x \rightarrow 1} \frac{x^2 - 1}{1 - x};$
2. $\lim_{x \rightarrow +\infty} (\sqrt{x-2} - \sqrt{x+3}), \quad \lim_{x \rightarrow +\infty} (\sqrt{x-2} - \sqrt{x^2+1}), \quad \lim_{x \rightarrow +\infty} (x - \sqrt{x^2-3});$
3. $\lim_{x \rightarrow +\infty} \left(1 + \frac{a}{x}\right)^x, \quad \lim_{x \rightarrow +\infty} x \ln \left(1 + \frac{1}{x}\right);$
4. $\lim_{x \rightarrow 0} \frac{\ln(1+x)}{x}, \quad \lim_{x \rightarrow 0} \frac{e^x - 1}{x};$
5. $\lim_{x \rightarrow +\infty} \frac{\ln x}{a^x} \quad (a > 1), \quad \lim_{x \rightarrow +\infty} 3^x - x^3, \quad \lim_{x \rightarrow +\infty} \frac{x^7 - 1}{2^x}, \quad \lim_{x \rightarrow +\infty} \ln \left(\frac{3^x}{x^3}\right);$
6. $\lim_{x \rightarrow +\infty} \frac{x^2 2^x}{(1+x)(2^x - x)}, \quad \lim_{x \rightarrow 0^+} \frac{\ln \sqrt[3]{1+x}}{x}, \quad \lim_{x \rightarrow +\infty} \frac{\ln(x^2 + 1)}{5^x};$
7. $\lim_{x \rightarrow 0^+} \frac{\tan x}{\sqrt{x}}, \quad \lim_{x \rightarrow 0} \frac{\tan x - \sin x}{x^3}, \quad \lim_{x \rightarrow +\infty} \frac{x}{|\sin x|}.$